

ADVANCED PLACEMENT PHYSICS 2 TABLE OF INFORMATION

CONSTANTS AND CONVERSION FACTORS		UNIT SYMBOLS
Avogadro's number,	$N_0 = 6.02 \times 10^{23} \text{ mol}^{-1}$	ampere, A
Universal gas constant,	$R = 8.31 \text{ J}/(\text{mol} \cdot \text{K})$	coulomb, C
Boltzmann's constant,	$k_B = 1.38 \times 10^{-23} \text{ J/K}$	degree Celsius, °C
1 atmosphere of pressure,	$1 \text{ atm} = 1.0 \times 10^5 \text{ N/m}^2 = 1.0 \times 10^5 \text{ Pa}$	electron volt, eV
Coulomb constant,	$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2}$	farad, F
Proton mass,	$m_p = 1.67 \times 10^{-27} \text{ kg}$	hertz, Hz
Neutron mass,	$m_n = 1.67 \times 10^{-27} \text{ kg}$	joule, J
Electron mass,	$m_e = 9.11 \times 10^{-31} \text{ kg}$	kelvin, K
Elementary charge,	$e = 1.60 \times 10^{-19} \text{ C}$	kilogram, kg
Vacuum permittivity,	$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N} \cdot \text{m}^2)$	meter, m
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7} (\text{T} \cdot \text{m})/\text{A}$	mole, mol
1 electron volt,	$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$	newton, N
Planck's constant,	$h = 6.63 \times 10^{-34} \text{ J} \cdot \text{s} = 4.14 \times 10^{-15} \text{ eV} \cdot \text{s}$ $hc = 1.99 \times 10^{-25} \text{ J} \cdot \text{m} = 1240 \text{ eV} \cdot \text{nm}$	ohm, Ω
Speed of light,	$c = 3.00 \times 10^8 \text{ m/s}$	pascal, Pa
Wien's constant,	$b = 2.90 \times 10^{-3} \text{ m} \cdot \text{K}$	second, s
Stefan-Boltzmann constant,	$\sigma = 5.67 \times 10^{-8} \text{ W}/(\text{m}^2 \cdot \text{K}^4)$	tesla, T
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg} = 931 \text{ MeV}/c^2$	volt, V
Universal gravitational constant, $G = 6.67 \times 10^{-11} \text{ m}^3/(\text{kg} \cdot \text{s}^2) = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$		watt, W
Magnitude of the acceleration due to gravity at Earth's surface, $g = 9.8 \text{ m/s}^2$		
Magnitude of the gravitational field strength at Earth's surface, $g = 9.8 \text{ N/kg}$		

PREFIXES		
Factor	Prefix	Symbol
10^{12}	tera	T
10^9	giga	G
10^6	mega	M
10^3	kilo	k
10^{-2}	centi	c
10^{-3}	milli	m
10^{-6}	micro	μ
10^{-9}	nano	n
10^{-12}	pico	p

VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES							
θ	0°	30°	37°	45°	53°	60°	90°
$\sin \theta$	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1
$\cos \theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0
$\tan \theta$	0	$\sqrt{3}/3$	3/4	1	4/3	$\sqrt{3}$	∞

The following conventions are used in this exam unless otherwise stated:

- The frame of reference is inertial.
- Frictional forces are negligible.
- Strings, springs, batteries, wires, and meters are ideal.
- Resistors and lightbulbs are ohmic.
- Ideal gases are monatomic.
- The electric potential is zero at an infinite distance from an isolated point charge.
- Current is conventional current.
- Capacitors are air-filled ($\kappa = 1.0$).
- The small angle approximation is valid for single- and double-slit diffraction.

Equations	ELECTRICITY		Units
Coulomb's law (electric force)	$ \vec{F}_E = \frac{1}{4\pi\epsilon_0} \frac{ q_1 q_2 }{r^2} = k \frac{ q_1 q_2 }{r^2}$	$A = \text{area}$	m^2
Electric field (force on test charge)	$\vec{E} = \frac{\vec{F}_E}{q}$	$C = \text{capacitance}$	$F = C/V$
Electric field (around point charge)	$ \vec{E} = \frac{1}{4\pi\epsilon_0} \frac{ q }{r^2} = k \frac{ q }{r^2}$	$d = \text{distance}$	m
Electric potential energy (system of 2 charges)	$U_E = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r} = k \frac{q_1 q_2}{r}$	$E = \text{electric field}$	$\text{N/C} = \text{V/m}$
Difference in potential energy	$\Delta U_E = q\Delta V$	$F = \text{force}$	$\text{N} = \text{kg}\cdot\text{m/s}^2$
Electric potential (from multiple point charges)	$V = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i}$	$I = \text{current}$	A
Average electric field	$ \vec{E} = \left \frac{\Delta V}{\Delta r} \right $	$\ell = \text{length}$	m
Capacitance	$C = \frac{Q}{\Delta V}$	$P = \text{power}$	$\text{W} = \text{J/s} = \text{N}\cdot\text{m/s}$
Capacitance (parallel-plate capacitor)	$C = \kappa\epsilon_0 \frac{A}{d}$	$q = \text{charge}$	C
Electric field (parallel-plate capacitor)	$E_C = \frac{Q}{\kappa\epsilon_0 A}$	$Q = \text{charge}$	C
Electric potential energy (capacitor)	$U_C = \frac{1}{2} Q\Delta V$	$r = \text{distance, radius, or position}$	m
Current	$I = \frac{\Delta q}{\Delta t}$	$R = \text{resistance}$	Ω
Resistance	$R = \frac{\rho\ell}{A}$	$t = \text{time}$	s
Electric power	$P = I\Delta V$	$U = \text{potential energy}$	$\text{J} = \text{kg}\cdot\text{m}^2/\text{s}^2$
Ohm's law	$I = \frac{\Delta V}{R}$	$V = \text{electric potential}$	$\text{V} = \text{J/C}$
Equivalent resistance (resistors in series)	$R_{\text{eq},s} = \sum_i R_i$	$\kappa = \text{dielectric constant}$	(no unit)
Equivalent resistance (resistors in parallel)	$\frac{1}{R_{\text{eq},p}} = \sum_i \frac{1}{R_i}$	$\rho = \text{resistivity}$	$\Omega\cdot\text{m}$
Equivalent capacitance (capacitors in series)	$\frac{1}{C_{\text{eq},s}} = \sum_i \frac{1}{C_i}$	$\tau = \text{time constant}$	s
Equivalent capacitance (capacitors in parallel)	$C_{\text{eq},p} = \sum_i C_i$		
Time constant (RC circuit)	$\tau = R_{\text{eq}} C_{\text{eq}}$		

Equations

Magnetic force (moving charge)

$$F_B = qvB \sin \theta$$

Magnetic field
(current-carrying wire)

$$B = \frac{\mu_0 I}{2\pi r}$$

Magnetic force (on wire)

$$F_B = I\ell B \sin \theta$$

Magnetic flux

$$\Phi_B = \vec{B} \cdot \vec{A}$$

$$\Phi_B = |\vec{B}| \cos \theta |\vec{A}|$$

Faraday's law
(induced emf)

$$|\mathcal{E}| = \left| \frac{\Delta \Phi_B}{\Delta t} \right|$$

Induced emf (moving rod loop)

$$\mathcal{E} = B\ell v$$

MAGNETISM

A = area

B = magnetic field

F = force

I = current

ℓ = length

q = charge

r = distance, radius, or position

t = time

v = velocity or speed

$\mathcal{E}$ = emf

θ = angle

Φ = flux

Units

m^2

$\text{T} = \text{N}/(\text{A}\cdot\text{m})$

$\text{N} = \text{kg}\cdot\text{m}/\text{s}^2$

A

m

C

m

s

m/s

$\text{V} = \text{J/C}$

deg

$\text{T}\cdot\text{m}^2 = \text{V}\cdot\text{s} = \text{Wb}$

THERMAL PHYSICS

Pressure

$$P = \frac{F_{\perp}}{A}$$

Average kinetic energy
(gas particles)

$$K_{\text{avg}} = \frac{3}{2} k_B T = \frac{1}{2} m v_{\text{rms}}^2$$

Heat transfer rate
(conduction)

$$\frac{Q}{\Delta t} = \frac{kA\Delta T}{L}$$

Ideal gas law

$$PV = nRT = Nk_B T$$

Internal energy
(ideal monatomic gas)

$$U = \frac{3}{2} nRT = \frac{3}{2} Nk_B T$$

Work done on a system

$$W = -P\Delta V$$

1st law of thermodynamics

$$\Delta U = Q + W$$

Energy to change temperature

$$Q = mc\Delta T$$

A = area

c = specific heat

F = force

k = thermal conductivity

K = kinetic energy

L = length

m = mass

n = number of moles

N = number of atoms

P = pressure

Q = energy transferred to
a system by heating

t = time

T = temperature

U = internal energy

v = velocity or speed

V = volume

W = work done on a
system

m^2

$\text{J}/(\text{kg}\cdot\text{K})$

$\text{N} = \text{kg}\cdot\text{m}/\text{s}^2$

$\text{W}/(\text{m}\cdot\text{K})$

J

m

kg

mol

(no unit)

$\text{Pa} = \text{N}/\text{m}^2$

J

s

K

J

m/s

m^3

$\text{J} = \text{N}\cdot\text{m}$

Equations

WAVES, SOUND, AND OPTICS

Units

Wavelength

$$\lambda = \frac{v}{f}$$

a = width

m

Index of refraction

$$n = \frac{c}{v}$$

A = amplitude

m

Snell's law (refraction)

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

d = separation

m

Thin lens or mirror

$$\frac{1}{s_i} + \frac{1}{s_o} = \frac{1}{f}$$

D = path length

m

Magnification

$$|M| = \left| \frac{h_i}{h_o} \right| = \left| \frac{s_i}{s_o} \right|$$

f = frequency or focal length

Hz = 1/s
or m

Path length diff. (bright fringes)

$$\Delta D = m\lambda$$

F = force

N = kg·m/s²

Path length diff. (single-slit)

$$\Delta D = a \sin \theta$$

h = height

m

Single-slit diffraction
(minima, dark fringes)

$$a \left(\frac{y_{\min}}{L} \right) \approx m\lambda$$

ℓ = length

m

Path length diff. (double-slit)

$$\Delta D = d \sin \theta$$

L = distance

m

Double-slit interference
(maxima, bright fringes)

$$d \left(\frac{y_{\max}}{L} \right) \approx m\lambda$$

m = order or mass

(no unit) or kg

Wave speed
(in a string)

$$v_{\text{string}} = \sqrt{\frac{F_T}{m/\ell}}$$

M = magnification

(no unit)

Period

$$T = \frac{1}{f}$$

n = index of refraction

(no unit)

Wave (displacement vs time)

$$x(t) = A \cos(\omega t) = A \cos(2\pi f t)$$

s = position

m

Wave (displacement vs position)

$$y(x) = A \cos\left(2\pi \frac{x}{\lambda}\right)$$

t = time

s

Beat frequency

$$|f_{\text{beat}}| = |f_1 - f_2|$$

T = period

s

v = speed

m/s

x = position

m

y = position

m

λ = wavelength

m

θ = angle

deg

ω = angular frequency

rad/s

Equations

Energy (photon)

$$E = hf$$

de Broglie wavelength
(particles)

$$\lambda = \frac{h}{p}$$

Wavelength (photon)

$$\lambda = \frac{c}{f}$$

Wien's law
(blackbody radiation)

$$\lambda_{\max} = \frac{b}{T}$$

S-B law (blackbody radiation)

$$P = A\sigma T^4$$

Photoelectric effect

$$K_{\max} = hf - \phi$$

Compton scattering

$$\Delta\lambda = \frac{h}{m_e c} (1 - \cos\theta)$$

Mass-energy equivalence

$$E = mc^2$$

Radioactive decay

$$N = N_0 e^{-\lambda t}$$

Decay constant
(half-life)

$$\lambda = \frac{\ln 2}{t_{1/2}}$$

MODERN PHYSICS

A = area

E = energy

f = frequency

K = kinetic energy

m = mass

N = number of particles

p = momentum

P = power

t = time

T = absolute temperature

θ = angle

λ = wavelength or decay
constant

ϕ = work function

Units

m^2

J

$\text{Hz} = 1/\text{s}$

J or eV

kg

(no unit)

$\text{kg}\cdot\text{m/s}$

$\text{W} = \text{J/s}$

s

K

deg

m

or $1/\text{s}$

J or eV

GEOMETRY AND TRIGONOMETRY

Rectangle

$$A = bh$$

Rectangular Solid

$$V = \ell wh$$

Triangle

$$A = \frac{1}{2}bh$$

Cylinder

$$V = \pi r^2 \ell$$

$$S = 2\pi r \ell + 2\pi r^2$$

Circle

$$A = \pi r^2$$

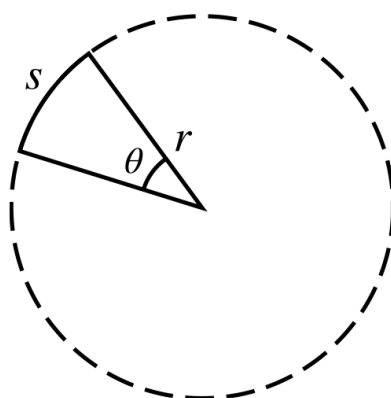
$$C = 2\pi r$$

$$s = r\theta$$

Sphere

$$V = \frac{4}{3}\pi r^3$$

$$S = 4\pi r^2$$



A = area

b = base

C = circumference

h = height

ℓ = length

r = radius

s = arc length

S = surface area

V = volume

w = width

θ = angle

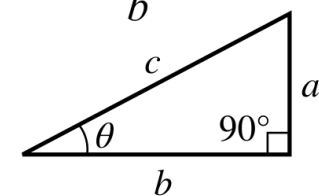
Right Triangle

$$a^2 + b^2 = c^2$$

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$



Equations

MECHANICS AND FLUIDS

Units

Linear kinematics

$$v_x = v_{x0} + a_x t$$
$$x = x_0 + v_{x0} t + \frac{1}{2} a_x t^2$$
$$v_x^2 = v_{x0}^2 + 2 a_x (x - x_0)$$

- a = acceleration
- d = distance
- E = energy
- F = force
- J = impulse
- k = spring constant
- K = kinetic energy
- m = mass
- p = momentum
- P = power
- r = radius or distance
- t = time
- U = potential energy
- v = velocity or speed
- W = work
- x = position
- y = vertical position
- θ = angle
- μ = coefficient of friction

- m/s²
- m
- J
- N
- kg·m/s = N·s
- N/m
- J
- kg
- kg·m/s
- W = J/s = N·m/s
- m
- s
- J
- m/s
- J = N·m
- m
- m
- deg or rad
- (no unit)

Center of mass

$$\vec{x}_{\text{cm}} = \frac{\sum m_i \vec{x}_i}{\sum m_i}$$

Newton's 2nd law

$$\vec{a}_{\text{sys}} = \frac{\sum \vec{F}}{m_{\text{sys}}} = \frac{\vec{F}_{\text{net}}}{m_{\text{sys}}}$$

Gravitational force

$$|\vec{F}_g| = G \frac{m_1 m_2}{r^2}$$

Friction force

$$|\vec{F}_f| \leq |\mu \vec{F}_N|$$

Spring force (Hooke's law)

$$\vec{F}_s = -k \Delta \vec{x}$$

Centripetal acceleration

$$a_c = \frac{v^2}{r}$$

Translational kinetic energy

$$K = \frac{1}{2} m v^2$$

Work

$$W = F_{\parallel} d = F d \cos \theta$$

Work-energy theorem

$$\Delta K = \sum W_i = \sum F_{\parallel, i} d_i$$

Spring potential energy

$$U_s = \frac{1}{2} k (\Delta x)^2$$

Gravitational potential energy

$$U_G = -\frac{G m_1 m_2}{r}$$
$$\Delta U_g = m g \Delta y$$

Power

$$P_{\text{avg}} = \frac{W}{\Delta t} = \frac{\Delta E}{\Delta t}$$
$$P_{\text{inst}} = F_{\parallel} v = F v \cos \theta$$

Linear momentum

$$\vec{p} = m \vec{v}$$

Impulse

$$\vec{F}_{\text{net}} = \frac{\Delta \vec{p}}{\Delta t} = m \frac{\Delta \vec{v}}{\Delta t} = m \vec{a}$$
$$\vec{J} = \vec{F}_{\text{avg}} \Delta t = \Delta \vec{p}$$

Velocity of center of mass

$$\vec{v}_{\text{cm}} = \frac{\sum \vec{p}_i}{\sum m_i} = \frac{\sum m_i \vec{v}_i}{\sum m_i}$$

Equations

MECHANICS AND FLUIDS

Units

Rotational kinematics

$$\omega = \omega_0 + \alpha t$$
$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$
$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$$

a = acceleration

m/s²

A = amplitude or area

m or m²

d = distance

m

f = frequency

Hz = 1/s

F = force

N

h = height

m

I = rotational inertia

kg·m²

k = spring constant

N/m

K = kinetic energy

J

ℓ = length

m

L = angular momentum

kg·m²/s

m = mass

kg

M = mass

kg

P = pressure

Pa = N/m²

r = radius or distance

m

t = time

s

T = period

s

v = velocity or speed

m/s

V = volume

m³

W = work

J = N·m

x = position

m

y = vertical position

m

α = angular acceleration

rad/s²

θ = angle or angular position

rad or deg

ρ = density

kg/m³

τ = torque

N·m

ω = angular speed

rad/s

Linear / rotational kinematics conversions

$$v = r\omega$$
$$a_T = r\alpha$$

Torque

$$\tau = r_{\perp} F = rF \sin \theta$$

Rotational inertia

$$I = \sum m_i r_i^2$$

Parallel axis theorem

$$I' = I_{\text{cm}} + Md^2$$

Newton's 2nd law (rotation)

$$\alpha_{\text{sys}} = \frac{\Sigma \tau}{I_{\text{sys}}} = \frac{\tau_{\text{net}}}{I_{\text{sys}}}$$

Rotational kinetic energy

$$K = \frac{1}{2} I \omega^2$$

Work (rotation)

$$W = \tau \Delta \theta$$

Angular momentum

$$L = I \omega$$
$$L = rmv \sin \theta$$

Angular impulse

$$\Delta L = \tau \Delta t$$

Center of mass (rolling)

$$\Delta x_{\text{cm}} = r \Delta \theta$$

Period

$$T = \frac{1}{f}$$

Mass-spring period

$$T_s = 2\pi \sqrt{\frac{m}{k}}$$

Pendulum period

$$T_p = 2\pi \sqrt{\frac{\ell}{g}}$$

Simple harmonic motion

$$x = A \cos(2\pi ft)$$
$$x = A \sin(2\pi ft)$$

Density

$$\rho = \frac{m}{V}$$

Pressure

$$P = \frac{F_{\perp}}{A}$$
$$P = P_0 + \rho gh$$
$$P_{\text{gauge}} = \rho gh$$

Buoyant force

$$F_b = \rho V g$$

Conservation of flow rate

$$A_1 v_1 = A_2 v_2$$

Bernoulli's equation

$$P_1 + \rho g y_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g y_2 + \frac{1}{2} \rho v_2^2$$