

# LEC 10 / week 5:- Principle of Resolution.

Clauses. Premise.

1) Order.

2) Sequence.

3) Equivalences.

Proof an Argument.

→ Disjunction ( $\vee$ ) of literals is called a clause.

→ literal = a Variable or its negation.

$$P \rightarrow \text{literal}$$

$$\neg P \rightarrow \text{literal}$$

$$\underline{\neg P \vee Q} = \text{a clause.}$$

$$\underline{\neg P \vee Q \vee R \vee S \vee T} = \text{a clause.}$$

$$P \rightarrow Q \neq \text{a clause.}$$

$$P \wedge Q \neq \text{a clause.}$$

$P_1 \rightarrow C_1$  one or more clauses.

$P_2 \rightarrow C_2$  by repeatedly

$P_3 \rightarrow C_3$  apply PR if

$\vdots$  we reach to

$P_n \rightarrow C_n$  an empty clause

$\therefore C$   $\therefore \neg C$

This means that

an argument is correct.

Step 1:- You will need to obtain clauses.

Step 2:- You will take negation of conclusion to make a clause.

a clause.

steps:- Repeatedly apply PR.

P1 → P  
 P2 → P → q  
 C → ∴ q

P → C1. X  
 $\neg P \vee q$  → C2. X  
 $\neg q$  → C3. X

from (C1, C2)  $q$  → C4. X  
 from (C3, C4)  $\square$  ✓ → C5

$\square$  = empty clause. Hence proved

Ex 11 Step 1:- Propositions.

P65 Step 2:- Logical Expressions.

P1 → T → (MVE)  $\neg T \vee MVE$  — C1  
 P2 → S → TE  $T S \vee TE$  — C2  
 P3 → TAS T — C3  
 C → ∴ M. S — C4  
 $\neg M$  — C5

from (C1, C2)  $\neg T \vee M \vee T S$  — C6  
 from (C3, C6)  $M \vee T S$  — C7  
 from (C4, C7) M — C8  
 from (C5, C8)  $\square$  — C9

Hence proved.

clauses.

$P \vee q$   $\neg$  Disjunctive.  
 $\Rightarrow$  you are lucky.

$P \wedge q = P$   
 $= q$

$P \rightarrow q = \neg P \vee q$

truth table.

$P \rightarrow q = \neg P \vee q$

Ex 6 P1 →  $\neg P \wedge q$   $\neg P$  — C1 X  
 62. P2 →  $r \rightarrow p$   $q$  — C2

62.  $P_2 \rightarrow \gamma \rightarrow P$        $q \quad \text{---} \quad C_2$   
 $P_3 \rightarrow \neg \gamma \rightarrow S$        $\neg \gamma \vee P \quad \text{---} \quad C_3^X$   
 $P_4 \rightarrow \underline{S \rightarrow t}$        $\gamma \vee S \quad \text{---} \quad C_4^X$   
 $C \rightarrow \therefore t$        $\neg S \vee t \quad \text{---} \quad C_5^X$   
                                   $\neg t \quad \text{---} \quad C_6^X$

from  $(C_1, C_3)$        $\neg \gamma \quad \text{---} \quad C_7^X$   
 from  $(C_4, C_7)$        $S \quad \text{---} \quad C_8^X$   
 from  $(C_5, C_8)$        $t \quad \text{---} \quad C_9^X$   
 from  $(C_6, C_9)$        $\square \rightarrow$  the argument is correct.

Observation: It is not compulsory to process all the clauses. if you obtain empty that's enough

Ex 7  $P_1 \rightarrow P \rightarrow q$        $\neg P \vee q \quad \text{---} \quad C_1$   
 63:  $P_2 \rightarrow \neg P \rightarrow \neg$        $P \vee \neg \quad \text{---} \quad C_2$   
 $P_3 \rightarrow \underline{\gamma \rightarrow S}$        $\neg \gamma \vee S \quad \text{---} \quad C_3$   
 $C \rightarrow \therefore \neg q \rightarrow S$        $\neg q \quad \text{---} \quad C_4$   
                                   $\neg S \quad \text{---} \quad C_5$

from  $(C_1, C_2)$        $q \vee \neg \quad \text{---} \quad C_6$   
 from  $(C_3, C_6)$        $q \vee S \quad \text{---} \quad C_7$   
 from  $(C_4, C_7)$        $S \quad \text{---} \quad C_8$   
 from  $(C_5, C_8)$        $\square$  therefore the argument

$P \rightarrow q \vee \neg P \vee q$   
 $\neg(P \vee q) = \neg P \wedge \neg q$

is correct.

Ex 9:  $P \rightarrow L \rightarrow A$

$\neg L \vee A \quad \text{---}^X C1$

$P \rightarrow E \rightarrow \neg I$

$\neg E \vee \neg I \quad \text{---}^X C2$

$P \rightarrow A \rightarrow E$

$\neg A \vee E \quad \text{---}^X C3$

$C \rightarrow \therefore L \rightarrow \neg I$

$L \quad \text{---}^X C4$

$E \quad \text{---}^X C5$

from  $C1, C3 \quad \neg L \vee E \quad \text{---}^X C6$

from  $C4, C6 \quad \neg L \vee \neg I \quad \text{---}^X C7$

from  $C5, C7 \quad \neg I \quad \text{---}^X C8$

from  $C8 \quad \square \quad \text{---} C9$

therefore the argument is correct.

Solving Questions.

- 1) Propositions.
- 2) Expressions.
- 3) Clauses.
- 4) Applying PR (Repeatedly)

Expect a question in session.

When we try to prove something scientifically. Strongest

1) Mathematical proof.

→ Argument proof.

- Rules of Inference

→ PR.

2) Experiments.

3) An Example.

