

Ex 11
P51

if a person is female and is a parent, then this person is Someone's mother

→ Use predicates and quantifiers to express this.

for all x , x is a person, if x is a female, and x is a parent, then

Domain is set of all people.

there exist y , y is a person, x is the mother of y

let $F(x) = x$ is a female

$P(x) = x$ is a parent

$M(x,y) = x$ is the mother of y .

Step 1 - Domain
Step 2 - Variables
Step 3 - it complete form-

$$\forall x (F(x) \wedge P(x)) \rightarrow \exists y (M(x,y)).$$

Ex 12
P52

Every one has exactly one best friend.

Domain consist of all people/persons.

for all x , x is a person, if there exist y , x is a friend of y , then

for all other people z , z is a person. x is not a friend of z .

$$\forall x \exists y F(x,y) \rightarrow \forall z \neg F(x,z).$$

$F(x,y) = x$ is a friend of y .

Q9
54

Everybody loves Jerry

domain all people in world.

for all x , x is a person, x loves Jerry

$L(x,y) = x$ loves y .

$L(x, Jerry) = x$ loves Jerry

$$\forall x L(x, Jerry).$$

Q10
54 (b) Every body loves Some body.

for all x , x is a person, there exist y , y is a person.

54 $\forall x \exists y$ for all x , x is a person, there exist y , y is a person.
 x loves y .

$$\forall x \exists y L(x, y)$$

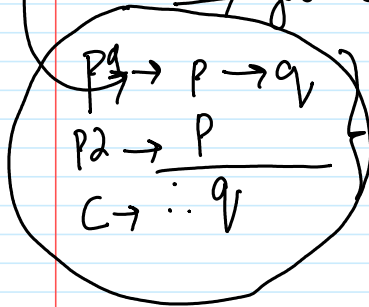
$$L(x, y) = x \text{ loves } y$$

RULES of Inference.

59) \rightarrow if you have a current password then you may log into the network.
 P q

\rightarrow you have the current password.
 therefore

\rightarrow you can log into the network



Alternate way of expressing.

Argument: premises followed by conclusion.

Correct argument:-

Fallacy:-

P_1
 P_2
 P_3
 \vdots

$$(P_1 \wedge P_2 \wedge P_3 \wedge \dots \wedge P_n) \rightarrow C$$

= Tautology

Valid argument.

fallacy.

$\therefore C$ } Conclusion.

$P_1 \rightarrow P \rightarrow q$
 $P_2 \rightarrow P$
 $C \rightarrow q$

$$(P_1 \wedge P_2) \rightarrow C$$

$$((P \rightarrow q) \wedge P) \rightarrow q \quad \checkmark \text{ valid.}$$

P	q	$P \rightarrow q$	$(P \rightarrow q) \wedge P$	$((P \rightarrow q) \wedge P) \rightarrow q$
T	T	T	T	T
T	F	F	F	T
F	T	T	F	T
F	F	T	F	T

T T F F | T F F F | (T T T T) ⇒ Tautology

Ex. 1) $\sqrt{2} > \frac{1}{2}$ then $(\sqrt{2})^2 > (\frac{1}{2})^2$
 $\sqrt{2} > \frac{3}{2}$ P: $\sqrt{2} > \frac{1}{2}$
 therefore Q: $(\sqrt{2})^2 > \frac{3}{2}$
 $(\sqrt{2})^2 > (\frac{3}{2})^2$

$$\frac{P \rightarrow Q}{P} \therefore Q$$

Basic Rules:-

- | | | | | | |
|---------|--|------------------------|---|---------------------------------------|-----------------|
| Table 1 | P | Modus Ponens | 5 | P | Addition. |
| 61 | ① $\frac{P \rightarrow Q}{\therefore Q}$ | | | $\frac{P}{\therefore P \vee Q}$ | |
| | ② $\frac{\neg Q}{P \rightarrow Q}$ | Modus Tollens | 6 | $\frac{P \wedge Q}{\therefore P}$ | Simplification. |
| | $\therefore \neg P$ | | | | |
| | ③ $\frac{P \rightarrow Q}{Q \rightarrow \neg P}$ | Hypothetical Syllogism | 7 | $\frac{P}{P \wedge Q}$ | Conjunction |
| | $\therefore P \rightarrow \neg P$ | | | | |
| | ④ $\frac{P \vee Q}{\neg P}$ | Disjunctive Syllogism | 8 | $\frac{P \vee Q}{\neg Q \vee \neg Q}$ | Resolution |
| | $\therefore Q$ | | | $\therefore P \vee \neg Q$ | |

Ex 2. "it is below freezing now", therefore "it is either below freezing or it is raining now!"

Sol:- P: it is below freezing.
 Q: it is raining now.

∴ it is a valid argument

$\therefore P \vee Q$ is a valid argument

$$\frac{P}{\therefore P \vee Q}$$
 it is a valid argument
Based on addition.

Ex4
b1 "it is below freezing and raining now"

therefore
"it is below freezing now."

p it is below freezing.

q it is raining now.

$$\frac{p \wedge q}{\therefore p}$$
 By Simplification this is
a valid argument.

Ex6
b2 "it is not sunny this afternoon and it is
colder than yesterday"

"we will go swimming only if it is sunny"

"if we do not go swimming then we will take a canoe trip"

"if we take a canoe trip then we will be home by sunset"

Leads to conclusion "we will be home by sunset"

p it is sunny this afternoon.

q it is colder than yesterday.

r we will go swimming.

s we will take a canoe trip.

t we will be home by sunset.

$P1 \rightarrow \neg p \wedge q$ — (1) X

$P2 \rightarrow r \rightarrow p$ — (2) X

$P3 \rightarrow \neg r \rightarrow s$ — (3) X

$P4 \rightarrow s \rightarrow t$ — (4) X

$C \rightarrow \therefore t$
↑

from (1) $\neg p$ — (5) X Using Simplification

from (2) r — (6) X Using Modus Ponens $\frac{p \wedge q}{\therefore p}$

from (3) s — (7) X Using Modus Ponens

from (4) t — (8) issue

$\hookrightarrow \therefore t$ $f(x) = t$ \rightarrow $\textcircled{8}$ using modus ponens.
and this is conclusions.

argument is valid.

fallacy \Rightarrow Unable to reach to conclusion.